

# Keeper # 28

## Solving Radical & Rational Exponent Equations

## Solving Radical Equation:?

- 1.) Isolate the radical on one side of the equation.
- 2.) Raise BOTH SIDES of the equation to the nth power. (nth power = index value)
- 3.) Simplify and solve.
- 4.) Check your solution(s) for extraneous solutions.

\*Solutions that cause the equation to be **FALSE**.

\*Can only occur when your index is **EVEN** and the isolated radical equals a **NEGATIVE** number.

$$\sqrt{\text{isolated}} = -\#$$

\*If your only solution is extraneous, then there is **NO SOLUTION**.

Example # 1: Solve

$$\sqrt{3x+1} - 3 = 1.$$

Example # 2: Solve.

$$\sqrt[3]{5 - 11x} = 3$$

Example # 3: Solve

$$2\sqrt[4]{4x-3} = -10$$

## Solving with Rational Exponents:

1.) Isolate the  $(\quad)^{\text{Rational Exponent}}$  on one side of the equation.

2.) Raise BOTH SIDES of the equation to the reciprocal of rational exponent.

$$\frac{2}{3} \rightarrow \frac{3}{2}$$

3.) Simplify and solve.

4.) Check your solution(s) for extraneous solutions.

\*Can only occur if your denominator is **EVEN** and the isolated  $(\quad)$  equals a **NEGATIVE** number.

$$(\quad)^{\text{Rational Exponent}} = -\#$$

Example # 4: Solve. Remember to check for extraneous solutions.

$$(x - 3)^{\frac{2}{3}} - 1 = 9$$

Example # 5: Solve. Remember to check for extraneous solutions.

$$-2(x + 4)^{\frac{1}{2}} + 3 = -5$$